



# Structure-from-Motion on shallow reefs and beaches: potential and limitations of consumer-grade drones to reconstruct topography and bathymetry

C. Gabriel David<sup>1</sup> · Nina Kohl<sup>1,2</sup> · Elisa Casella<sup>3</sup> · Alessio Rovere<sup>4</sup> · Pablo Ballesteros<sup>1</sup> · Torsten Schlurmann<sup>1</sup>

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**Abstract** Reconstructing the topography of shallow underwater environments using Structure-from-Motion—Multi View Stereo (SfM-MVS) techniques applied to aerial imagery from Unmanned Aerial Vehicles (UAVs) is challenging, as it involves nonlinear distortions caused by water refraction. This study presents an experiment with aerial photographs collected with a consumer-grade UAV on the shallow-water reef of Fuvahmulah, the Maldives. Under conditions of rising tide, we surveyed the same portion of the reef in ten successive flights. For each flight, we used SfM-MVS to reconstruct the Digital Elevation Model (DEM) of the reef and used the flight at low tide (where the reef is almost entirely dry) to compare the performance of DEM reconstruction under increasing water levels. Our results show that differences with the reference DEM increase with increasing depth, but are substantially larger if no underwater ground control points are taken into account in the processing. Correcting our imagery with algorithms that account for refraction did not improve the overall accuracy of reconstruction. We conclude that reconstructing shallow-water reefs (less than

1 m depth) with consumer-grade UAVs and SfM-MVS is possible, but its precision is limited and strongly correlated with water depth. In our case, the best results are achieved when ground control points were placed underwater and no refraction correction is used.

**Keywords** Bathymetry from drones · Bathymetry from photogrammetry · Structure from motion underwater · Coral reefs · Drone mapping

## Introduction

Coral reefs are complex and highly biodiverse ecosystems that are put at risk by increasing stresses from both local and global factors (Fine et al. 2019). In turn, they provide several ecosystem services amounting to nearly 200,000 US dollars per acre per year (Costanza et al. 2014). Natural hazards and anthropogenic pressures affect small islands' coastlines and the underwater marine environment surrounding them (Kench and Brander 2006; Duvat and Magnan 2019; David and Schlurmann 2020). In the face of climate change, the increase in ocean temperatures is forecasted to lead to more extensive coral bleaching (Skirving et al. 2019), causing increased coral mortality (Hédouin et al. 2020). As coral reefs play an important role in the protection of low-lying islands from waves and wave energy (Ferrario et al. 2014), it is important to develop and assess the effectiveness and precision of new and low-cost techniques to monitor the evolution of reef areas over time. To this end, remote sensing from satellites or laser scanners and echo sounders are often employed to analyze the status and temporal evolution of beaches and marine environments (Klemas 2011; Colbo et al. 2014; Hedley et al. 2018; Panagou et al. 2020).

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✉ C. Gabriel David  
david@lufi.uni-hannover.de  
https://www.lufi.uni-hannover.de

<sup>1</sup> Ludwig-Franzius-Institute for Hydraulic, Estuarine and Coastal Engineering, Leibniz Universität Hannover, Nienburger Str.4, 30167 Hannover, Germany

<sup>2</sup> Blue C GmbH, Hannover, Germany

<sup>3</sup> ZMT, Leibniz Center for Tropical Marine Research, Bremen, Germany

<sup>4</sup> MARUM, Center for Marine Environmental Sciences, University of Bremen, Bremen, Germany

Single-Beam Echo Sounder (SBES) or Multibeam Echo Sounder (MBES) sonar determine water depths by transmitting sound pulses into water. Survey grade MBES cover areas with a sensor covering a lateral area of  $120^\circ - 150^\circ$  to record bathymetry with a vertical resolution of  $< 1\%$  of the water depth (Colbo et al. 2014). However, survey-grade echo sounders depend on vessel draft and are usually not suitable for shallow waters ( $< 4-5$  m depth, Leon et al. 2015; David and Schlurmann 2020). Consumer-grade SBESs—for example used by fishers—have a smaller immersion depth but recorded water depths vary between centimeter to lower decimeter scale compared to ground-truth water depths (Bandini et al. 2018). Furthermore, SBESs record punctual measurements and thus do neither provide an areal overview of the surveyed marine area, nor color information for mapping of the site, which is particularly relevant in coral reefs.

Other bathymetric survey methods are operated from the beach: Terrestrial 60 Laser Scanning (TLS) can record topography and bathymetry from a single device. The error of underwater measurements increases with distance to the device. Here, the measuring error is equal to the measured water depth for distances  $\geq 15$  m (Panagou et al. 2020).

A further method to derive bathymetries of coastal zones is to observe nearshore wave propagation and transformation, both by radar (Borge et al. 2004; van Dongeren et al. 2008) and video (or high-frequency image) recording devices (Aarninkhof et al. 2005; Holman et al. 2013). Radar-based depth inversion methods require stationary installed devices and process data in the order of days (Chernyshov et al. 2020; Gawehn et al. 2020). In contrast, UAV-borne video data uses mobile equipment that can be controlled remotely. But in this case, operating times are limited, as they depend on battery capacities (Bergsma et al. 2019). Still, both techniques are especially valuable on sandy shores with turbid waters.

In clear waters however, aerial imagery has been applied to directly survey underwater topography or bathymetry. For example, recent studies, employing UAV-borne Light Detection and Ranging (LiDAR), achieved centimeter accuracy for riverine waters of less than 2 m depth (Mandlbürger et al. 2020). When using UAV-borne LiDAR measurements, bathymetric reconstruction is independent of surface texture. This leads to a more robust outcome compared to photogrammetric methods (Mandlbürger 2019). However, LiDAR-based data struggle with “*too shallow*” waters or increased hydrodynamic activity, such as whitecaps of broken waves (Klemas 2011; Leon et al. 2015). A major issue with UAV-borne LiDAR is that drone platforms carrying the devices are usually larger and have a high take-off weight, which often requires a higher-level drone operations permits. A more common way to employ UAV-borne data is therefore to use consumer-

grade drones, collecting aerial photographs and processing them with the SfM-MVS reconstruction approach afterward. SfM-MVS merges photogrammetric principles with advances in 3D computer vision algorithms (Carrivick et al. 2016).

The SfM-MVS methods use aerial imagery to create precise and accurate three-dimensional DEM of coastal areas (Murfit et al. 2017; Casella et al. 2020; Talavera et al. 2020). However, reconstructing coastal areas with SfM-MVS techniques is mostly limited to dry beach areas. Thorough planning in advance helps to identify the potentials and limitations under the given circumstances on site and to manage expectations of the achievable outcome (Joyce et al. 2019). SfM-MVS techniques have been applied widely to reconstruct coastal topography with centimeter accuracy (see for example Casella et al. 2016; Murfit et al. 2017; Casella et al. 2020; Talavera et al. 2020). As for underwater imagery, three-dimensional photogrammetric models facilitate to study changes in coral reefs (Storlazzi et al. 2016; Rossi et al. 2019; Carlot et al. 2020). Using airborne images to analyze underwater environments requires (a) calm water surfaces, (b) is dependent on the Secchi depth (visibility by means of turbidity) and (c) is dependent on surface textures of underwater areas (Mandlbürger 2019). Within the water column, light is continuously attenuated through absorption and scattering along the optical path (Chirayath and Earle 2016; Chirayath and Li 2019). Bathymetric reconstruction in calmer and deeper waters with user grade UAVs (and without LiDAR sensors) is possible, but is characterized by large uncertainties and becomes more challenging with increasing water depths and hydrodynamic activity (Casella et al. 2017). But the biggest challenge of UAV-borne photogrammetry on coasts is to include and exploit recordings of both, surface and underwater images from aerial imagery, because light refracts on the water surface (Casella et al. 2017; Dietrich 2017; Mandlbürger 2019). Refraction of light on the water surface is explained by Snell’s Law. Using Snell’s Law directly on submerged riverine areas of the reconstructed DEMs already reduces the error, while site specific calibrations can further improve results (Shintani and Fonstad 2017). Other approaches consider camera parameters and viewing angles in their refraction correction and improve the reconstruction precision to be about 0.02% of the flying altitude (Westaway et al. 2000; Woodget et al. 2015; Dietrich 2017). Recently, machine-learning algorithms have emerged, correcting consumer-grade UAV data of submerged areas with a corresponding subset of accurate point clouds from LiDAR measurements (Agrafiotis et al. 2019, 2020). This approach is similarly accurate than more sophisticated refraction correction based on Snell’s Law.

Through-water photogrammetry depends on calm water surfaces, as surface undulations further disturb the SfM-MVS process beyond the aforementioned effects. Further adverse effects from surface undulations include unwanted reflection of sunlight on the water surface—also known as sun glare—(Overstreet and Legleiter 2017; Muslim et al. 2019) and light effects on the seafloor. These light effects are caused by wave crests, which act as fluid lenslet. However, fluid lenslets also facilitate magnification of the seafloor in certain areas and benefit its three-dimensional reconstruction when using high-framerate multispectral videos (Chirayath and Li 2019). At the time of writing though, such fluid lensing algorithm is not publicly available, while readily available platforms are about ten times more expensive than user-grade UAVs (Chirayath and Earle 2016).

This study stems from a project dealing with sea level rise and associated impacts on small islands (Ratter et al. 2019; David and Schlurmann 2020). The project focuses on obtaining field measurements with aerial surveys to evaluate sediment transport as natural sea level rise adaptation on the Maldivian reef island of Fuvahmulah. While on-land (dry beach) areas were the main objective of the project, this work analyzes data collected on reef flats on Fuvahmulah. Error metrics for varying water depths on reef flats are currently not available (David and Schlurmann 2020). The purpose of this study is therefore to assess the quality of reconstructed underwater topographies (bathymetries) from a SfM-MVS algorithm for different water levels and thus to utilize this information in future studies. We used a consumer-grade drone to record the intertidal inner reef. We surveyed the same area in ten flights, with varying water depth conditions. We employed pressure sensors to constantly measure water depths and a Real-Time Kinematic (RTK) Global Navigation Satellite System (GNSS) system to measure the position of Ground Control Points (GCPs) throughout the entire study site with centimeter precision. The GCPs are later used to georeference the three-dimensional model, obtained through the SfM-MVS and Multi-View Stereo (MVS) approach. Surveying starts with the dry reef at low tide and continues as water levels increase with rising tide. In the analysis, the digital reconstruction of the dry reef serves as “accurate” reference topography. Comparing the dry reference DEM with all following DEMs under increasing water depths, we estimate errors of the SfM-MVS algorithm in the bathymetric reconstruction originating from increasing water depth. This study provides error estimates related to three different aligning techniques in the photogrammetric process and evaluates the bathymetric reconstructions calculated with and without the use of publicly available refraction correction algorithms.

Overall, this study aims at (a) assessing the potential and limitation of SfM-MVS algorithms to reconstruct underwater areas; (b) evaluating the benefits of refraction correction in near-shore coastal areas; and (c) increasing confidence in exploiting aerial imagery of clear, shallow waters for bathymetric reconstruction in photogrammetric procedures under field conditions.

## Study area, material and methods

### Survey site and area of interest

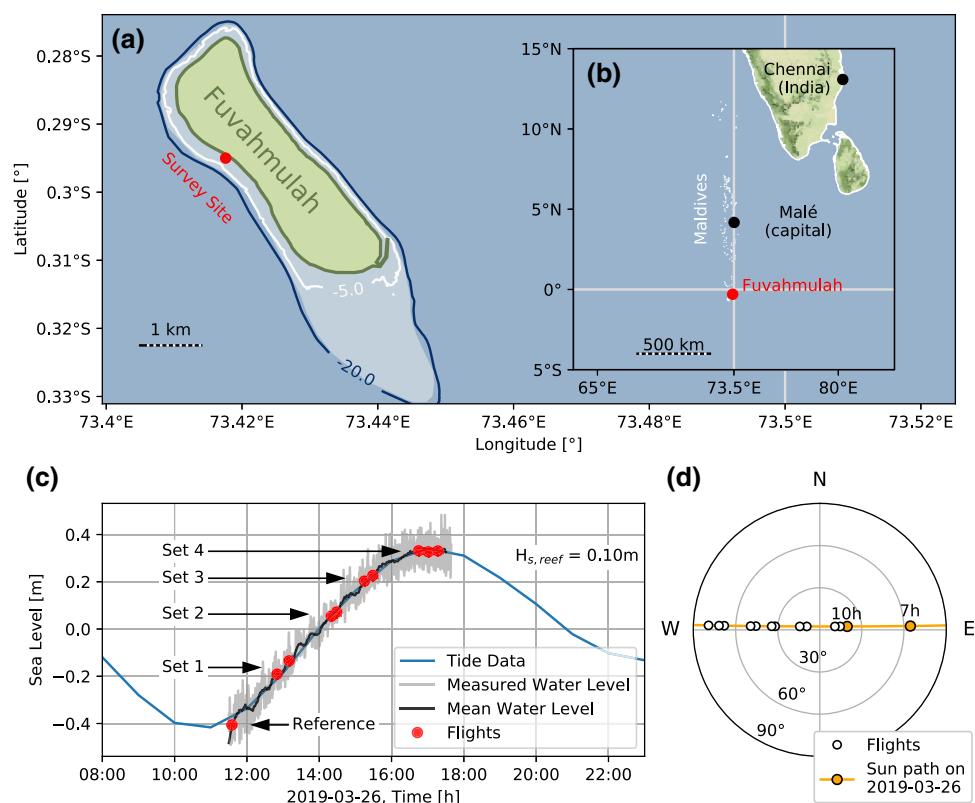
This study was carried out on the reef island Fuvahmulah, one of the most southern islands of the Maldives (Indian Ocean). The island is located about 30 km south of the equator (latitude:  $-0.30^\circ$ , longitude:  $73.43^\circ$ , see Fig. 1a). The capital of the Maldives Malé is situated approximately 500 km north of the island, while the distance to the southern tip of the Indian peninsula is about 1025 km (see Fig. 1b). Unlike most other inhabited atolls of the Maldives, Fuvahmulah only consists of one main island and its fringing reef.

This study distinguishes between the survey site and the area of interest: The survey site is the entire area recorded by the UAV. The area of interest focuses on the georeferenced area within the survey site (see Fig. 2).

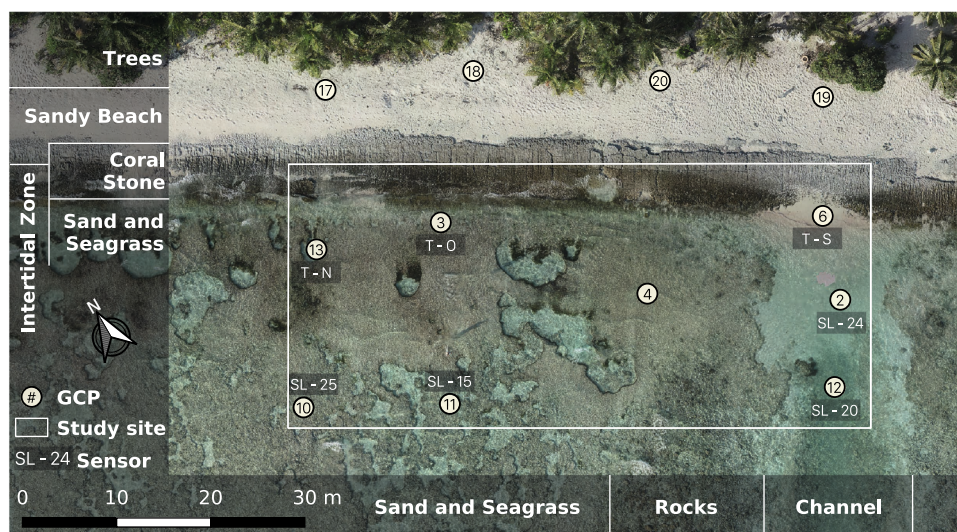
The survey site is on a shallow, inter-tidal reef on the west coast of Fuvahmulah. The water around Fuvahmulah is clear and provides aerial visibility of the submerged reef bottom—even in depths over 1 m. The study includes ten flights, recorded on March 26th, 2019 between low-tide at around 11:00 and high tide at around 17:30. The tidal range of spring tide in March 2019 was 1.21 m (all tide data from UHSLC; Caldwell et al. 2015). The tidal range on the survey day was 0.76 m, allowing the reef to fall dry at low tide. The water level on the reef  $\Delta h$  is the difference between the first flight and the water level of each subsequent flight, derived from the sea level data (Table 1 summarizes the different water levels and water depths on the study site for each flight). On the survey day, the sky was constantly clear and sunset was at 18:10 (Holmgren et al. 2018, pvlb v0.7.2). Thus, lighting on site only depends on the solar azimuth and zenith (Fig. 1d). For the survey day, the fifth-generation atmospheric reanalysis of the global climate (ERA5) of the Collaboration for Australian Weather and Climate Research (CAWCR) gives a significant off-shore wave height of 0.87 to 1.00 m at  $0^\circ$  latitude and  $73^\circ$  longitude (C3S 2017), which is at a distance of  $\sim 60$  km from Fuvahmulah.

The aerial surveys cover a distance of about 140–150 m long shore and 70–80 m cross-shore. Four cross-shore zones characterize the survey area: the upper beach is a

**Fig. 1 Geographic location and field conditions.** Location of **a** the study site on the island and **b** of Fuvahmulah within the Indian Ocean; **c** displays the sea level for the survey based on nearby tide data and water levels measured on site. On March 26th, 2019, the measured data and mean significant wave height on the reef  $H_{s,reef}$  is recorded by wave gauge SL-20 (see Fig. 2); **d** sun position on March 26, 2019, throughout the day (orange markers are exemplary times at 07:00 and 10:00 for orientation) at associated flight times (white marker, for exact times, see Table 1)



**Fig. 2 Survey site, study site and setup.** Orthophoto of the survey site on the reef, with reef areas classified according to their landform. The white border shows the study site within the survey site. Round circles show the ground control point (GCP) locations. GCPs paired with pressure sensors have a sensor identifier label below them



vegetated beach ridge, fringing the entire island. It hosts palm trees and shrubs (see Fig. 2). A sandy beach of  $\sim 10$  m width follows seaside of the vegetated area. The downward sloping coral stone delimits the sandy beach from the fringing coral reef. The coral stone experiences wave run-up and can be considered a natural revetment for the nearby beaches. It is located between about mean sea level and mean high waters. The inter-tidal reef has three longshore sections: On the right side, inhabitants of the island have cut a channel into the reef. The channel

provided safe landing for boats before the seaport opened in 2002 (Ratter et al. 2019; David and Schlurmann 2020). This area is constantly submerged and has the highest water depth of the study site. The channel bottom is sandy near the beach but becomes increasingly more rocky seaward. The excavated rocks from the channel construction were dumped adjacent to the channel along the entire reef width and remain there until today. In this longshore area, only the 15 m long inner reef flat section close to the beach is clear of excavated rocks. The remaining reef flat

**Table 1** Overview of water levels and average water depth on the reef within the study site (hydrostatic conditions). Sea level  $z_{SL}$  measurements at pressure sensor SL-20 (see Fig. 2); reef water level  $\Delta h$  refers to flight number 1, serving as reference case with  $\Delta h = 0$  m;

Set	Ref.	S1		S2		S3		S4		
Flight number	1	2	3	4	5	6	7	8	9	10
Sea level $z_{SL}$ [m]	-0.41	-0.19	-0.14	0.05	0.07	0.20	0.23	0.33	0.33	0.33
Reef water level $\Delta h^1$ [m]	0.00	0.22	0.27	0.46	0.48	0.61	0.63	0.74	0.73	0.74
Mean water depth $\bar{h}^2$ [m]	0.02	0.07	0.09	0.19	0.21	0.30	0.33	0.42	0.41	0.41
Local survey time	11:35	12:50	13:10	14:20	14:30	15:15	15:30	16:45	17:00	17:30

<sup>1</sup>Derived from sea level

<sup>2</sup>Averaged from measured water level over pressure sensors

on the left side consist of corals, sand and seagrass. On the landward side of the reef, seagrass grows on the corals and traps sand. Small ponds form in areas which lack seagrass and thus sand cover. These ponds remain submerged for the entire study.

The fringing reef attenuates incoming waves, but the area is still subject to water surface undulations. Sensor SL-20 (see Fig. 2) records the significant wave height—the sensor lies in the inundated channel and measures constantly throughout the entire field survey. The resulting significant wave height on the reef is  $H_s = 0.10$  m, calculated as the mean of the highest 33 m waves from a zero-crossing analysis.

The survey site contains 12 uniquely colored and labeled GCPs. These GCPs are made of 0.5 m wide square PVC-tarpaulin sheets. Later, in the SfM-MVS process, the GCPs serve as georeference and scaling of the point cloud and they are used in the bundle adjustment to optimize the image alignment. Therefore, each GCP's center position is measured with a survey grade GNSS system, being set up as base-rover combination for RTK measurements. Both GNSS devices are Septentrio AsteRx-U receiver combined with a NAVX-3G antenna. The devices measure the GCPs' position with an accuracy of  $1.24 \pm 0.14$  cm. An equal distribution of GCPs further supports the alignment quality: four GCPs cover the constantly dry sandy beach, while the remaining eight GCPs lie on the shoreward half of the intertidal reef flat. Seven of the eight reef GCPs are also paired with pressure sensors, measuring the water depth constantly (see Fig. 2). The sampling rate is between 1 Hz and 8 Hz for the four Seametrics PT2X sensors (ID: SL-number, in Fig. 2) and 16 Hz for the three DRIESEN + KERN P-Log3021-MMC sensors (ID: T-letter, in Fig. 2). The mean water depth  $\bar{h}$  is the average inundation of the reef during each flight, considering measurements from all pressure sensors. In this study, all water depths are measured on-site, while water levels are based on tide data

mean water depth  $\bar{h}$  on the reef as average submergence of the irregular reef bottom within the study site

from University of Hawaii Sea-Level Center (UHSLC, Caldwell et al. 2015).

### Digital elevation models

A DJI Phantom 4 Pro (V.1) quadcopter records aerial images in ten flights with 25 m altitude from the take-off location. Each flight is considered one survey, as every flight covers the entire survey area. Flight planning is done by DRONEDeploy, allowing to record images automatically every 2 s. To record the images, the drone carries a 20 megapixel camera with the camera angle at nadir position (perpendicular to the ground). With these settings, images overlap 80% in the front and 75% on the sides. To further improve three-dimensional reconstruction, all surveys—except number four to six—also contain images of the survey area in non-nadir position (DRONEDeploy option *3D Mode* turned on). While the first flight of the entire study is the reference flight over the dry reef, all other flights are clustered in four sets with two consecutive flights each—except for the last set containing three consecutive flights (see Table 1). Repeating flights in each set with similar boundary conditions creates redundancy and is meant to compensate for complications, such as deteriorated visibility. The time between the start of each set is about 45–75 min, while within each set, the time between the take-offs is 10–20 min (see Fig. 1c and Table 1).

The aerial images of each flight are the basis for a three-dimensional reconstruction, being carried out with METASHAPE (v1.5.3 Professional, build 8432; agisoft.com)—a commercial, proprietary software solution by AGISOFT LLC (Agisoft 2019) incorporating Structure-from-Motion (SfM, Westoby et al. 2012) and MVS algorithms (in the following referred to as SfM-MVS). The software uses the recorded aerial images of each flight to find clearly distinguishable points in two or more images (tie points; with SfM-MVS). Based on these points, METASHAPE aligns the

cameras. Afterward, the software uses the aligned aerial images to calculate a dense point cloud (with MVS) and then creates three-dimensional models, serving as base for the DEMs and orthophotos. This procedure is carried out for each flight (see Table 1), resulting in ten models. In this study the DEMs of each model have a resolution of 1.36–1.76 cm px<sup>-1</sup> and the associated orthophotos have a resolution of 0.68–1.31 cm px<sup>-1</sup>. The quality setting for each reconstruction step in METASHAPE are set to high (see Appendix, Table 3 for further information on settings in METASHAPE). Conventional SfM-MVS techniques make use of self-calibrating bundle adjustment, to accurately handle nonmetric or consumer-grade camera data in photogrammetric processes (Moniwa 1981). But these self-calibrating bundle adjustments are not able to account for radial lens distortion, so that aerial images with almost parallel viewing perspectives contain systematic broad-scale errors in the photogrammetric process—usually referred to as “(vertical) doming”, which has been analyzed by James and Robson (2014). Using simulations of multi-image networks, James and Robson (2014) show that self-calibration, as part of the bundle adjustment process, leads to systematic errors in the DEM and can be mitigated by following practical flight plan solutions: (a) avoiding self calibration (if an accurate camera model is available), (b) taking images with off-nadir camera orientation, (c) estimating the parameter value associated with minimal systematic DEM error using suitably distributed control points (James and Robson 2014; Meinen and Robinson 2020). Other authors showed that the presence and the distribution of GCPs are relevant in reducing the doming effect. In fact, in the area where GCPs are dominant, the elevation difference is an order of magnitude smaller when compared to other regions in the DEM (Nesbit and Hugenholtz 2019; Casella et al. 2020). Camera calibration and correction routines can improve, but not fully diminish systematic errors—especially in peripheral regions of the DEMs (Girod et al. 2017). In this sense, the photogrammetric reconstruction of the reef from images of flight 4 leads to more pronounced doming than observed in any other reconstruction within this study—probably because the survey only contained images recorded in nadir orientation (images in non-nadir position were not collected for flight 4) and sun glint on aerial images affect the photogrammetric process adversely (see Appendix, Fig. 6). Sun glint is another error source in aerial images, impairing the three-dimensional reconstruction of the scene (Overstreet and Legleiter 2017). A polar filter on the camera lens can reduce the effect of sun glint on water surfaces and several techniques for high-resolution UAV imagery exist, using near-infrared wavelengths (700–1000 nm) to account for this effect (Muslim et al. 2019). However, recording

information from these wavelengths requires special sensors, usually not being deployed on user-grade UAVs. In flight 4, the sun glint appeared on the upper, north–west facing border in almost all aerial images of the water surface, despite using a polar filter. As a result, sun glint affected the overlapping area between images—and thus the photogrammetric reconstruction—adversely. Due to the obvious and more pronounced vertical errors within the imagery of flight 4, data from this flight will not be considered in the further evaluation of this study. In addition, the SfM-MVS algorithm struggles to provide elevation data in areas being subject to stronger water surface undulations (mostly in the channel, see Fig. 2). At high tide, the pressure sensors record the highest hydrodynamic activity (Fig. 1c). With the SfM-MVS algorithm’s interpolation disabled, 2–4% of the pixels of the flights at high tide (flights 8–10) had no elevation information.

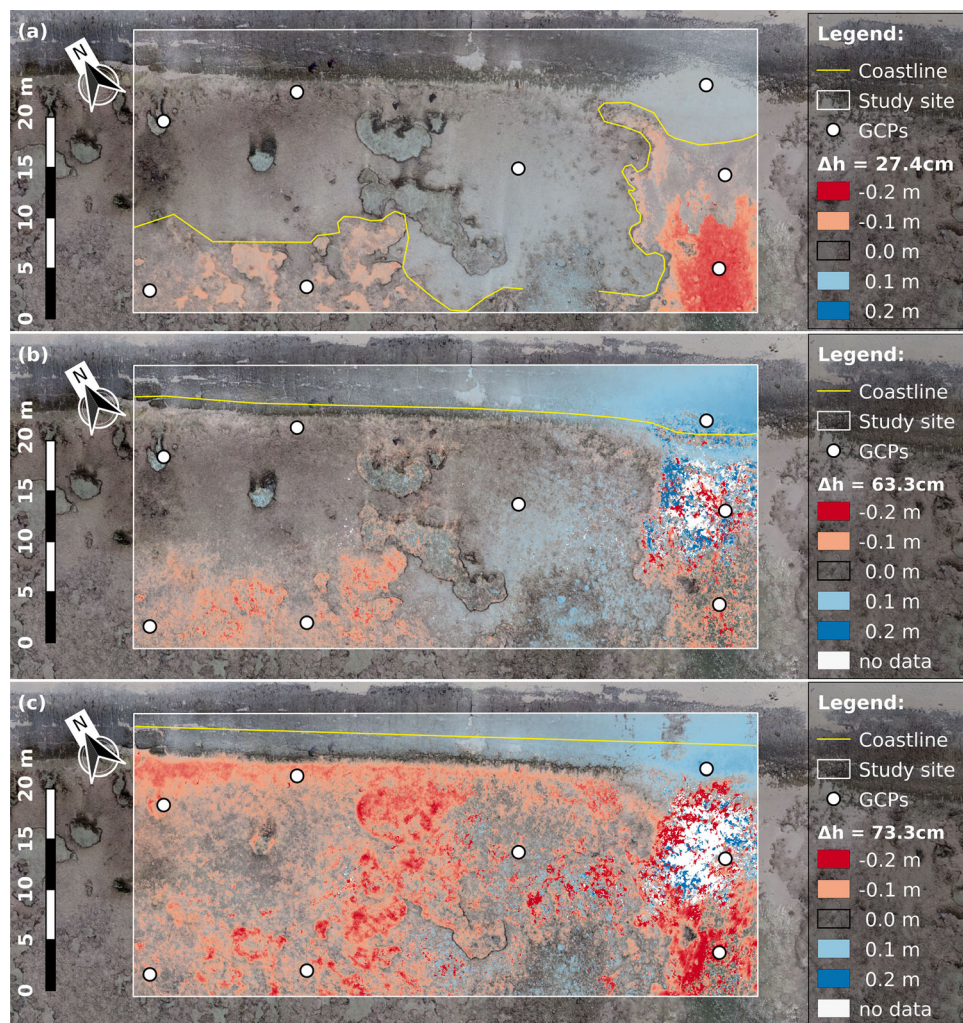
The first flight captures the dry reef and serves as reference case for all following flights. All following flights will record the site under rising tide and thus higher water levels. Acknowledging deviations between coordinates in DEMs and independent measurements (Casella et al. 2020), in this study the dry reef’s DEM is the most exact reconstruction of the reef. Therefore, the resulting deviation DEM ( $\Delta$ DEM) describes the error made by the SfM-MVS algorithm in underwater areas as:

$$\Delta\text{DEM}_i = \text{DEM}_{\text{surface},1} - \text{DEM}_{\text{inundated},i} \quad (1)$$

with the dry reference  $\text{DEM}_{\text{surface},1}$  of flight 1 and the gradually inundated topographies  $\text{DEM}_{\text{inundated},i}$ . The index  $i$  accounts for the subsequent flights 2–10 (see Table 1). Consequently, calculating the deviation between the dry reference DEM and those from an increasingly inundated area reveals the ability of the SfM-MVS algorithm to reconstruct underwater topography for different water levels. Despite that all error metrics derived in this study rely on the reference case  $\text{DEM}_{\text{surface},1}$ , the variability among reconstructions from consecutive flights over the dry reef is negligible (for more detailed information on this see Appendix). With regard to  $\Delta$ DEM, negative values mean the SfM-MVS algorithm considers the area to be shallower than the actual dry topography and vice-versa positive values show deeper waters. The raster calculation was carried out in QGIS (version 3.10 LTR “A Coruña” and 3.16 “Hannover”; [qgis.org](http://qgis.org)). The software used its internal nearest neighbor algorithm to resample the different DEM resolutions to a common resolution of 1.8 cm px<sup>-1</sup> in all  $\Delta$ DEMs.

We consider three survey methods that have an impact on the alignment procedure in the photogrammetric process:

**Fig. 3**  $\Delta$ DEMs for flight 3, 7 and 9. Difference between the initial, dry DEM and **a** the submerged DEMs with **a**  $\Delta h = 0.274$  m (flight 3), **b**  $\Delta h = 0.633$  m (flight 7), and **c**  $\Delta h = 0.733$  m (flight 9) in the study area. Red values indicate shallower water depths in the reconstruction and vice versa blue areas show areas being reconstructed higher than in the reference, dry reef model. Differences range between  $\pm 20$  cm. The yellow lines are the coastlines, manually extracted from orthophotos and aerial images (see Appendix, Fig. 7)



- The first approach considers the area of interest to be fully accessible and uses all available—even submerged—GCPs in the alignment.
- The second approach uses submerged, “wet” GCPs only (see Appendix, Table 4). It considers all DEMs from flight 5 onward, as the reef flat (sandy area with seagrass in Fig. 2) is fully submerged in these cases.
- The third approach is done by assuming that only dry areas were accessible (also disregarding the submerged GCPs no.12 in the channel and no. 13 lying in a pond in reconstructions of earlier flights). As the water level increases, GCPs becoming wet are also neglected in the associated alignment (for more information, see Appendix, Table 4).

Furthermore, we also present two different approaches to analyze the error made by the SfM-MVS algorithm in underwater areas as:

The first method illustrates the rastered  $\Delta$ DEMs over the reference flight’s orthophoto, giving a more

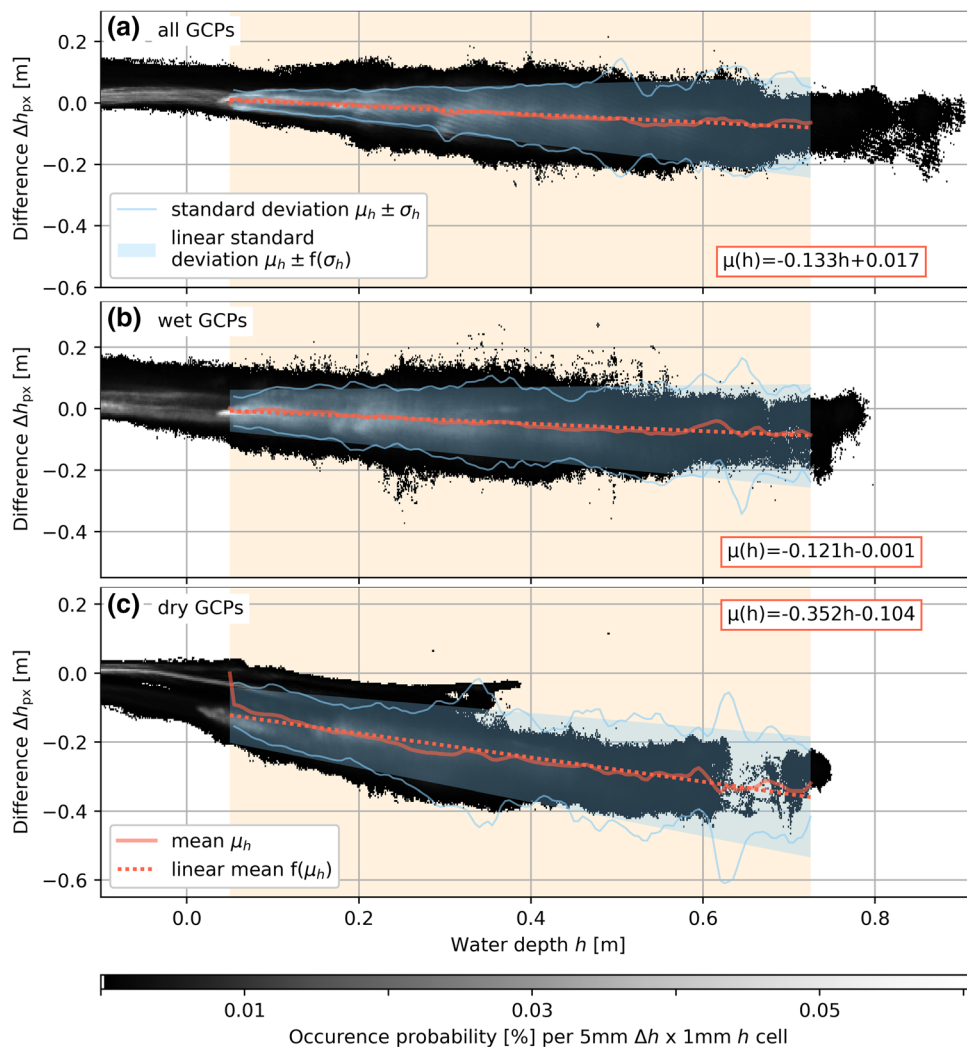
straightforward overview of the reconstruction error for each survey and its associated reef water level  $\Delta h$  separately (Fig. 3).

Another, more integral approach considers the data of all surveys at once: Since  $\Delta$ DEM indicates the error made by the SfM-MVS algorithm in underwater areas, pairing the error  $e_{px}$  of each pixel in every  $\Delta$ DEM with the pixels’ associated water depth  $h_{px}$  yields a water depth-dependent representation of the reconstruction error (carried out in PYTHON v.3.7.4 with the modules RASTERIO v.1.1.3 and Fiona v.1.8.13 post). Here, the water depth at each pixel  $h_{px}$  is derived from the pixel’s z-coordinate and its mean water depth on the reef  $\bar{h}$  for each flight (see Table 1).

Combining the data from all nine  $\Delta$ DEMs results in about  $2 - 3 \cdot 10^7$  data points. To illustrate this sheer amount of point data, two-dimensional histograms analyze the error occurrence probability over water depth (Figs. 4, 5 in results). These two-dimensional histograms employ a 5 mm by 1 mm raster ( $h_{px}$  by  $e_{px}$ ), yielding 1.1 million combinations of  $h_{px}$  and  $e_{px}$  (python module: MATPLOTLIB,

**Fig. 4 Performance of underwater reconstruction.**

The figure combines the occurrence probability of depth differences  $e_{px}$  between the reference DEM and the submerged DEMs with the associated water depths  $h$  in the study area. **a** illustrates the results for DEMs being aligned with all GCPs, **b** with DEMs considering only submerged (“wet”) and **c** only surface (“dry”) GCPs. A linear regression  $\mathcal{O} = 1$  for each case summarizes the scatter plots by giving a function  $\mu(h)$  of the mean deviation in dependence of the depth. The function is valid in the range of 0.05–0.73 m



v3.1.3 with function *hist2d*). The according mean elevation difference  $\bar{e}_h$  combines all  $e_{px}$  in one water depth  $h$ -bin of the histogram as

$$\bar{e}_h = \frac{1}{N_h} \sum_{n=1}^{N_h} e_{px,n} \tag{2}$$

with  $N_h$  as number of  $e_{px}$  per  $h$ -bin of the histogram. Based on the two-dimensional histograms, a regression function of  $\bar{e}$  summarizes the mean error as function of the water depth  $h$ , hence giving a general water depth-dependent error estimate for photogrammetric reconstruction of inundated areas:

$$\mu(h) = y + \sum_{o=1}^{\mathcal{O}} m_o \cdot h^o \tag{3}$$

with  $\mathcal{O}$  as order of the regression function,  $m_o$  as estimated coefficients for the regression problem and  $y$  as the function’s intercept of the ordinate (python module: `SCIKIT-LEARN v0.21.3`, with `LinearRegression` function for  $\mathcal{O} = 1$

and `PolynomialFeatures` function for  $\mathcal{O} > 1$ ). The coefficient of determination  $R^2$  expresses the regression function’s quality to approximate the mean elevation difference of each bin  $\bar{e}_{h,b}$ :

$$R^2 = 1 - \frac{\sum_{b=1}^{B_h} (\bar{e}_{h,b} - \mu(h)_b)^2}{\sum_{b=1}^{B_h} (\bar{e}_{h,b} - \bar{e}_h)^2} \tag{4}$$

with  $B_h$  as number of bins,  $\bar{e}_{h,b}$  as true value  $\bar{e}_h$  in each bin  $b$  and  $\mu(h)_b$  as the predicted value of  $\bar{e}_{h,b}$  using the water depth  $h$  in the regression function (in Eq. 4,  $\bar{e}_h$  is the mean of  $\bar{e}_h$ , calculated analogously to Eq. 2 for all bins  $b$  of  $B_h$ ). If  $R^2 = 1$ , the regression function predicts the mean elevation difference  $\bar{e}_h$  perfectly.  $R^2$  decreases when the relationship worsens and for  $R^2 = 0$  the regression function disregards any of the provided input features (the  $R^2$  score function comes from the python module `SCIKIT-LEARN` version 0.21.3). In this study, the regression functions are valid between the water depth limits  $h = 5$  cm and  $h = 73$  cm. The lower end is defined by the amplitude  $a$  of



the significant wave height with  $a = 0.5H_s$ , while the upper end correlates to the maximum water level on the reef  $\Delta h_{max}$  (see Table 1). The root-mean-square error RMSE between the regression function and the each pixel's elevation difference  $e_{px}$  from the survey is

$$\text{RMSE} = \sqrt{\frac{1}{N_{px} - 1} \sum_{n=1}^{N_{px}} (e_{px} - \mu(h_{px}))^2} \quad (5)$$

with  $N_{px}$  as all considered pixels from every  $\Delta$ DEMs (python module: SCIKIT-LEARN with *mean\_squared\_error* function and option *squared = False*). In this study, the root-mean-square error measures the quality of the regression function to represent the data. In turn, the regression function itself (Eq. 3) is a metric, expressing the depth-dependent deviation made by the photogrammetric process to reconstruct underwater bathymetry in comparison to “dry” surface topography.

### Refraction correction

Snell's law describes the main challenge and error source of airborne SfM-MVS to reconstruct bathymetry: a submerged object reflects light, traveling to the camera which then records the optical information in an aerial image. However, as the light travels through two media, it refracts at the water surface, altering how inundated areas appear on the image (Woodget et al. 2015; Dietrich 2017). Snell's law is the mathematical description of underwater objects, appearing to be shallower from outside the water:

$$n_{\text{air}} \cdot \sin(\theta_{\text{air}}) = n_{\text{water}} \cdot \sin(\theta_{\text{water}}) \quad (6)$$

with  $n_{\text{air}}$  as refractive index of air (1.0 in Dietrich 2017),  $n_{\text{water}}$  as refractive index of water (1.337 for fresh water in Dietrich 2017),  $\theta_{\text{air}}$  as incident- and  $\theta_{\text{water}}$  as refraction angle (nadir to SfM-MVS point). Snell's equation accounts for the systematic underprediction of water depths in airborne imagery. Therefore, recent studies used Eq. 6 and presented attempts correcting optical refraction and improving SfM-MVS in underwater areas (Woodget et al. 2015; Dietrich 2017; Chirayath and Instrella 2019). For example, the PYTHON-based, open-source algorithm `PY_SFM_DEPTH` (Dietrich 2017) builds on existing approaches (Woodget et al. 2015) and provides an additional processing step to `METASHAPE`. The algorithm reverse-engineers the vertical underwater position of the submerged dense points by applying Snell's law on the point's apparent locations. To achieve this, `PY_SFM_DEPTH` uses the information of each point's cameras (location and orientation) as well as an interpolated, plain water level—similar to the calculation of  $h_{px}$  in this study. `PY_SFM_DEPTH` is designed for shallow and calm inland waters without using

underwater GCPs to align the point cloud (Dietrich 2017). According to the homepage of `PY_SFM_DEPTH`, the refraction correction provides the best outcome with (a) clear water, (b) as few as possible reflections, and (c) minimal water surface undulations (Dietrich 2020). The homepage also predicts that waves will “increase the ‘noise’ in the SfM point cloud [... and] lead to inaccuracies/errors in the final outputs”. With this in mind, the present study tests the refraction correction algorithm `PY_SFM_DEPTH` for coastal waters under site-specific wave impact with aerial images from flights 6 and 10 (with mean reef water depths  $\Delta h$  of 0.61 m and 0.74 m, see Table 1). The refraction coefficient used within the refraction correction is  $n_{\text{water}} = 1.337$  (as suggested by Dietrich 2017). The resulting two-dimensional histograms are based on about  $4.4 - 4.5 \cdot 10^6$  data points (Fig. 5).

### Results

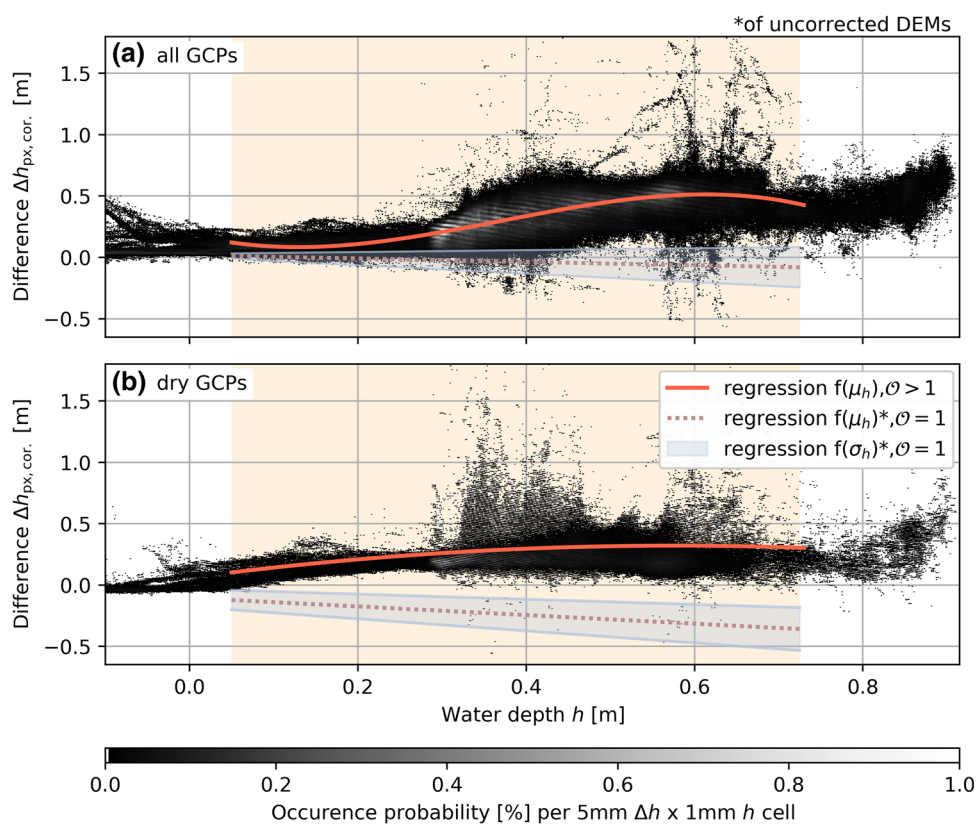
As outlined in the methods, this study tests three survey approaches: in the first approach, the reef is accessible and surface, as well as underwater GCPs can be recorded. In the second approach, only underwater GCPs are taken into account in the photogrammetric procedure, while in the third approach only the dry areas are considered to be accessible and thus submerged GCPs are disrespected. The next section presents results from the native workflow with `METASHAPE`—both with and without refraction corrected depths. The following section contains the same procedure with refraction corrected models.

#### Bathymetric reconstruction with submerged and dry GCPs

The first analysis of bathymetric reconstruction assumes that the reef is accessible and underwater GCPs can be recorded. Here, the SfM-MVS algorithm uses all GCPs in the alignment step of the reconstruction. The result is the orthophoto of the reference dry topography, combined with data from all  $\Delta$ DEMs (see Fig. 3). The  $\Delta$ DEMs contain the differences between the dry and submerged reef from two of the ten flights. Following Snell's Law (Eq. 6), negative values imply the actual, dry reef  $\text{DEM}_{\text{surface}}$  appear to be lower than on the submerged  $\text{DEM}_{\text{inundated},i}$  and vice versa for positive values. In general, the results confirm the initially suggested deviation and underpredicted water depths of submerged areas by Snell's law (Eq. 6). Also, the largest differences between the reconstructions of the dry and wet reef occurs in the deeper channel on the right side. Especially for areas subject to more hydrodynamic activity—especially breaking waves—the SfM-MVS algorithm does

### Fig. 5 Performance of underwater reconstruction with refraction correction.

The figure combines the occurrence probability of depth differences  $e_{px,corr}$  between the reference DEM and the refraction corrected, submerged DEMs with the associated water depths  $h$  in the study area. **a** illustrates DEMs considering all GCPs and **b** the results for DEMs being only aligned with dry surface GCPs. The scatter plots of the refraction corrected DEMs are best summarized by higher order regression functions  $\mu(h)$  with  $\mathcal{O} > 1$ . The results are plotted against the linear regression with  $\mathcal{O} = 1$  from Fig. 4a to visualize the error scale compared to the uncorrected reconstruction. The functions are valid in the range of 0.05–0.73 m



not always find matching points, leading to no-data patches in the  $\Delta$ DEMs (white areas in Fig. 3b and c).

However, the central area of the study site stands in contrast to the general results: The water depth in the shallower area of the DEM is overestimated when not or only slightly submerged ( $\Delta h = 0.274$  m and  $0.633$  m, Fig. 3a and b). This area is slightly shallower than the adjacent areas on the left (see photos in Appendix, Fig. 7). Some rocky outcrops remain above the water level and defining a definite coastline is difficult in this area (see Fig. 3a). But even the DEM with the highest submergence (Fig. 3c) still eventually contains small spots being over-predicted, albeit all rocky outcrops are submerged. Also, the area above the channel is constantly overestimated for all submergence levels. These results show that the SfM-MVS algorithm forces the submerged areas to match the inundated GCPs, negatively affecting adjacent dry areas.

The results from the orthophotos only give insights into each particular flight. Calculating the specific water depth of each pixel and combining it with the measured difference of water depth gives an integrated view over all flights. This method presents the SfM-MVS algorithm's performance to reconstruct underwater areas. The test case using submerged GCPs in the alignment phase results in  $30.5 \cdot 10^6$  data points, facilitating a probabilistic estimation of errors (see Fig. 4). For water depths  $h$  between 0.05 and 0.73 m the bathymetry is increasingly overestimated by a

rate of  $-13.2 \pm 21.7\%$  of the water depth (see Fig. 4a). The corresponding linear function of

$$\mu(h) = -0.132h + 0.017 \quad (7)$$

describes this trend with the water depth  $h$  and a root-mean-square error of  $\text{RMSE} = 0.008 \pm 0.027$  m ( $R^2 = 0.91$ ). If only submerged GCPs are considered in the alignment (see Fig. 4b), the function changes to

$$\mu(h) = -0.121h - 0.001 \quad (8)$$

The function has a root-mean-square error of  $\text{RMSE} = 0.011 \pm 0.025$  m with the goodness of fit being  $R^2 = 0.84$ .

If the submerged reef was not accessible, only dry surface GCPs could be used in the alignment. This prevents the SfM-MVS algorithm to force the submerged areas on the GCPs. As the water level increases, the number of GCPs available for aligning decreases. Therefore—and as expected from Snell's Law (Eq. 6)—the underwater reconstruction for this approach is less accurate and the errors increase to  $-35.2 \pm 13.9\%$  of the water depth for this study (see Fig. 4c, based on  $19.9 \cdot 10^6$  points). The linear function of the regression analysis is

$$\mu(h) = -0.352h - 0.104 \quad (9)$$

The function yields a root-mean-square error of  $\text{RMSE} = 0.030 \pm 0.075$  m between 0.05 and 0.73 m water depth ( $R^2 = 0.86$ ).

### Refraction correction

Recent attempts successfully corrected water depths from aerial images in riverine environments (Westaway et al. 2000; Woodget et al. 2015), for example with an additional processing step after the alignment (Dietrich 2017).

Using only surface GCPs shows an inverse behavior of the reconstruction error between the corrected and uncorrected DEMs when compared to the previous approach of using all GCPs: with the refraction correction applied, the error is now positive, meaning the correction reconstructs the inundated areas deeper than they are in the reference DEM (Fig. 5). The uncorrected reconstruction, using both surface and underwater GCPs or only underwater GCPs, improves the reconstruction error compared to using only dry, surface GCPs (Fig. 5a, based on  $4.5 \cdot 10^6$  points). However, when using the refraction correction, aligning the point cloud with both surface and underwater GCPs appears counterproductive. The regression analysis approximates the increased error with the function

$$\mu(h) = 1.705h^3 - 2.802h^2 - 1.581h + 0.001 \quad (10)$$

The function is valid in the range of 0.05–0.73 m with a RMSE of 0.194 m ( $R^2 = 0.98$ ). But when using only dry surface GCPs and applying a refraction correction (Fig. 5b, based on  $4.4 \cdot 10^6$  points), the errors remain relatively constant when water depths increase beyond 0.5 m. This is in accordance with the method's expected error behavior of being dependent on the flying altitude (Dietrich 2017). The regression analysis for the present case approximates the performance with the function

$$\mu(h) = -0.805h^2 + 0.921h + 0.056. \quad (11)$$

The function yields a root-mean-square error of  $\text{RMSE} = 0.271$  m for water depths  $h$  between 0.05 and 0.73 m ( $R^2 = 0.84$ ).

Regarding the absolute error of the reconstruction without underwater GCPs and of the refraction corrected reconstruction including submerged GCPs (Figs. 4a, 5a), both methods perform about equally well for water depths between 0.10 and 0.55 m. Beyond depths of 0.55 m the error by the refraction correction stabilizes, while it increases for the uncorrected DEMs.

Therefore, despite being subject to sub-par field conditions, the bathymetric reconstruction benefits from the refraction correction in deeper waters, when no underwater GCPs are used. However, the SfM-MVS algorithm still

aligns the bathymetry more exactly with submerged GCPs than correcting an unaligned bathymetry.

### Discussion and conclusion

In photogrammetry, when light refracts on the water surface, submerged objects appear distorted on airborne images, leading to falsely estimated water depths in SfM-MVS algorithms. This study quantifies these errors with data from a specially designed field experiment. Our results show the SfM-MVS algorithm underestimates underwater areas by  $13.2 \pm 21.7\%$  (see Fig. 4) of the water depth when both surface and submerged GCPs are used in the optimization process. The result does not significantly improve ( $12.1 \pm 15.3\%$ ) when considering only submerged GCPs. But in both cases, reconstruction accuracy of adjacent surface areas decreases with this method. Without using submerged GCPs in the optimization process, the error is at  $35.2 \pm 13.9\%$  of the water depths and the reconstruction benefits from refraction correction in waters deeper than 0.55 m.

In our example, the uncorrected reconstruction leads to underestimated water depths while the corrected reconstruction overestimated the submergence. Despite a varying order  $\mathcal{O}$  in the approximation of the error function  $\mu(h)$  (see Eq. 3 as well as Figs. 4, 5), future studies should clarify if the reconstruction for water depths up to  $\approx 1$  m in general benefit from combining the corrected and uncorrected approach. However, beyond water depths of  $\approx 1$  m, the uncorrected reconstruction would impair the refraction correction's relatively stable performance in deeper waters (Fig. 5).

Comparing airborne photogrammetry with other methods to obtain bathymetries (for example LiDAR, echo sounder, etc.) reveals that SfM-MVS algorithms provide good estimates of shallow water depth as well as mapping abilities for clear waters with low hydrodynamic activity. This study, however, uses the approach in more challenging environments and utilizes data recorded under field conditions: The survey was carried out on a sunny day with low winds, which can be considered normal for the late dry season in the Maldives. Also, the off-shore wave height  $H_s$  of 0.88–1.00 m is normal for Fuvahmulah in March, albeit lower than average (David and Schlurmann 2020). The fringing reef attenuates these waves, but the study site still experiences hydrodynamic activity—for example in the form of bores, surges, wave run-up, etc. (Monismith 2007)—which increases as the tide rises. The statistical zero-crossing method used here to calculate  $H_s$  does not consider the smaller surface waves traveling on ondular bores (Sous et al. 2019) but represents the sea state reasonably well compared to qualitative observations on site.

Still, waves in the study area affect the results in several aspects:

- Reconstructing underwater scenes suffers from light effects such as sun glint or reflections on the plain water surface as well as caustics, which are brighter areas from wave-induced fluid lenslets focussing sunlight on the seafloor (Casella et al. 2017; Dietrich 2017; Overstreet and Legleiter 2017; Chirayath and Li 2019; Muslim et al. 2019). If the water surface changes while recording, the incident and reflection angle change in Snell's Law. As consequence, the SfM-MVS algorithm get ambiguous information on an object's location and shape, which impairs the reconstruction and can fail to give any information for these areas (see *no data* areas in Fig. 3).
- Ambiguous information impacts the refraction correction even stronger than it affects SfM and MVS, since the refraction correction relies stronger on camera position and orientation to emend the appearing depth to the actual depth of each underwater dense point. This ambiguity results in more noise (as described in the manual of PY\_SFM\_DEPTH). In addition, the algorithm PY\_SFM\_DEPTH considers a plain water surface to compute refraction correction. This is not the case in coastal waters, leading to increased errors when compared to riverine environments with calmer water surfaces (compare the results of Dietrich 2017 with this study's results for the refraction correction in Table 2). This underlines that the quality of the refraction correction highly benefits from calm waters, improving mapping of submerged structures. However, even with waves present, it still enhances the bathymetric reconstruction without underwater GCPs.
- Water surface undulations also impact the mean water level estimation, used to calculate the water depth  $h$  of each pixel in  $\Delta$ DEM, as well as for the refraction correction. Both use an averaged water level derived from the measurements in the study site, neglecting the spatiotemporal variation of  $h$  within each flight (compare water levels  $\Delta h$  at sensor SL-20, Table 1). In the absence of water level measurements, the plain water level for the refraction correction could be estimated by sampling the water edge on a river's bank (Dietrich 2020). However, this post-processing step is less accurate on beaches, because they experience wave run-up. With wave run-up, the coastline is varying and therefore, manual water edge or coastline detection is

**Table 2 Summary and context of results.** Bathymetric drone surveys in literature and associated accuracy metrics in comparison to results of this study

Study	Water depth	Difference <sup>a</sup>	Deviation	Notes
Westaway et al. (2000)	< 0.6 m	0.04–0.15 m	±0.09–0.23 m	Refraction correction; riverine
Woodget et al. (2015)	< 0.2 m	0.05–0.09 m	0.07–0.09 m	Uncorrected, submerged; riverine
	< 0.2 m	0.01–0.05 m	0.06–0.09 m	Refraction correction; riverine
Casella et al. (2017)	< 1.8 m	0.02 m	±0.45 m	Native; submerged reef
Ye et al. (2016)	"Inner Reef"	0.68 m	0.62 m	Water depth unspecified; reef
Dietrich (2017)	< 1.8 m	0.02% flying altitude		Refraction correction; riverine
Shintani and Fonstad (2017)	≤ 1.2 m	0.17–0.18 m <sup>†</sup>	0.18 m	Native; riverine environment
	≤ 1.2 m	0.13–0.14 m <sup>†</sup>	0.17–0.19 m	Directly corrected water depths
Agrafiotis et al. (2020)	≤ 5.6 m	0.19 m	0.28 m	Machine learning (ML) procedure
	≤ 4.1–6.9 m	0.02–0.06 m	0.09–0.14 m	ML; nearshore (calm seas)
	≤ 14.8 m	0.04 m	0.37 m	ML; nearshore (calm seas)
Genchi et al. (2020)	~ 1 m <sup>†</sup>	0.18–0.22 m		Native; estuarine, beach
Casella et al. (2020)	Only surface	0.005 to 0.21 m		Literature overview; dry beaches
This study	< 0.74 m	13.3% water depth	±21.7%	Surface and underwater GCPs; reef
	< 0.74 m	12.1% water depth	±15.3%	Only underwater GCPs; reef
	< 0.74 m	35.2% water depth	±13.9%	No underwater GCPs; reef
	< 0.74 m	~ 1.0% flying altitude		Refraction correction; reef

<sup>a</sup>Root-mean-square error if not stated otherwise

• Mean absolute error

<sup>†</sup>Estimated from figure, but unspecified in article

more difficult and somewhat more arbitrary in coastal areas.

- In practical terms, the results of this study suggest the best workflow for reconstructing aerial imagery of coastal areas is to separate surface and shallowly submerged areas if sufficient GCPs in inundated areas exist. The bundle adjustment in the SfM-MVS algorithm corrects the sparse point cloud to match the GCPs, having a negative effect on adjacent areas (see Figs. 3, 4a and b, where submerged, wet GCPs affect surface areas negatively and vice versa for Fig. 4c).

The aim of this study was to scrutinize the performance of user-grade UAVs used for topographic reconstruction of coastal areas and associated sediment volumes. Coastal environments consist of surface and underwater areas. SfM-MVS has been successfully used before to create DEMs of dry coastal topography with errors in the order of centimeters (Casella et al. 2020), but through-water photogrammetry is still prone to inaccuracies due to the inherent physical challenges—especially when waves disturb the water surface. Sophisticated approaches use the fluid lensing effect of waves as an advantage to provide high-quality reconstruction of underwater areas (Chirayath and Earle 2016; Chirayath and Li 2019). But such numeric procedure is not (yet) widely available. Other refraction correction algorithms exist, which also aim at improving the precision and accuracy of bathymetric reconstructions from aerial imagery (see Table 2). If complementary, sparse bathymetric measurements from echo-sounding or LiDAR sensors exist, machine learning procedures support SfM-MVS algorithms for submerged areas up to about 15 m water depths in clear water conditions (Agrafiotis et al. 2019, 2020). Without any preparations or post-processing, SfM-MVS algorithm natively facilitates bathymetric reconstruction and aerial mapping of shallowly inundated areas, albeit the reconstruction error increases with water depth and hydrodynamic activity (see Table 2 or Casella et al. 2017; Ye et al. 2016; Shintani and Fonstad 2017; Genchi et al. 2020). However, a confident error metric of standard SfM-MVS has been missing for in field campaigns in coastal surveys or on coral reefs with user-grade UAVs. Therefore, this study quantifies the depth-dependent error in a typical field campaign environment. The results encourage to extent surface (“dry”) beach surveys with conventional UAVs beyond the coastline. The reconstruction improves from adapting aligning strategies, which can already be considered in the planning of the field campaign or pragmatically adapted to the conditions on

site. If field conditions do not allow for improved GCP placement, aerial imagery of submerged areas can still be utilized in a SfM-MVS algorithm, but DEMs of these areas contain higher errors. Beyond a depth of 0.55 m, reconstruction of underwater areas further benefits from refraction correction when post-processing the field data. But the reconstruction remains vulnerable to disturbances by waves and sun reflections. In these cases, further correction of the aerial images is required or more advanced techniques, such as fluid lensing, should be considered.

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**Authors’ contribution** CGD planned the survey with input from EC and AR. PB and AR prepared the devices. PB provided the data from the hydrodynamic measurements. CGD, NK and PB carried out the field campaign. CGD and NK post-processed the data with help and advice from EC and AR. CGD prepared the manuscript with the help of NK. EC, AR and TS edited and contributed to the final manuscript. AR and TS designed the research projects in the research program and funded this study.

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#### Declarations

**Conflict of interest** The authors declare that they have no conflict of interest.

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## Appendix

### Photoscan settings

The study used the SfM and MVS algorithms provided by the software METASHAPE (v1.5.3 Professional, build 8432; [agisoft.com](http://agisoft.com)) to calculate three-dimensional DEM of the increasingly submerged reef flat and adjacent beach area. METASHAPE provides several settings, influencing different stages of the SfM-MVS procedure. Table 3 contains the settings used in METASHAPE for this study.

**Table 3 Settings to create the digital elevation model.** Settings and values in METASHAPE used throughout this study. Here, ✓ means, the option is enabled in the software, while disabled options are marked with X. Values set to 0 do not prescribe a value, but allow the software to find a value itself

Processing step	Setting	
Alignment	Accuracy	High
	Reset current alignment	✓
	Reference preselection	X
	Generic preselection	X
	Key point limit	0 (zero)
	Tie point limit	0
	Adaptive camera model fitting	X
Dense point cloud	Quality	High
	Depth filtering	Aggressive
	Reuse depth maps	X
	Calculate point colors	✓
Mesh	Source data	Dense cloud
	Surface type	Height field
	Depth maps quality	Medium
	Face count	High
	Custom face count	200 000
	Interpolation	Disabled
	Point classes	All
	Calculated vertex colors	✓
	Reuse depth maps	X
	Use strict volumetric masks	X
	DEM	Source data
Interpolation		Disabled
Point classes		All
Use custom region		X
Orthomosaic	Resolution (m)	0
	Surface	Mesh
	Blending mode	Mosaic
	Hole filling	✓
	Enable back-face culling	X
	Refine seamlines	X
	Use custom region	X

### Sun glint in aerial images

The method sections shortly touch upon the removal of flight 4 from this study, due to stronger doming than in reconstructions of other flights. Possible reasons are the absence of off-nadir images and strong and structural sun glint on the aerial images. Sun glint in aerial images results in very bright pixels from reflections of sun light on the water surface (Overstreet and Legleiter 2017). Figure 6 shows one aerial image from flight 4, containing sun glint on the upper, northwest facing border of the image process.

### Reference digital elevation model

All error metrics in this study rely on the first flight serving as reference case. The SfM-MVS software returns a reconstruction error, quantifying the quality of the sparse point cloud to match the GCPs. This error is 5.6 cm in the first reference flight. Since the area does not contain any Independent Control Points (ICPs), there is no accuracy metric for the reconstruction, but it is in comparable studies, it is usually within centimeter scale (Casella et al. 2020).

To check the variability of the reconstruction, we used a test flight preceding the experiments of this study. The test flight while the GCPs were placed and the pressure sensors installed, to check the functionality of the UAV and the quality of the preplanned flight. In this test flight, all GCPs were already in place, instead of those on the sandy beach with the numbers 17-20. We did a reconstruction of this flight and compared the resulting reconstruction of the study site to the reconstruction of the first flight. To ensure comparability among both reconstructions, we have not used GCPs 17 to 20 in the reconstruction of flight 1. We



**Fig. 6 Sun glint in an aerial image.** Sun glint in one aerial image, recorded within flight 4. This type of sun glint also appears on almost all other aerial images of flight 4, showing the water surface. The sun glint is on the images' northwest facing border and thus affects image overlapping within the photogrammetric

**Table 4** Dry GCPs GCPs that are dry (●) or wet (◊) in the respective flight sets

Position within survey site <sup>a</sup>	Beach				Water line			Center		Sea ward		
	17	18	19	20	13	3	6	2	4	10	11	12
GCP number												
Reference set <sup>b</sup>	●	●	●	●	◊	●	●	●	●	●	●	◊
Flight set 1	●	●	●	●	◊	●	●	◊	●	●	◊	◊
Flight set 2	●	●	●	●	◊	◊	●	◊	◊	◊	◊	◊
Flight set 3	●	●	●	●	◊	◊	●	◊	◊	◊	◊	◊
Flight set 4	●	●	●	●	◊	◊	◊	◊	◊	◊	◊	◊

In this table, the GCPs are sorted according to their location in Fig. 2, starting from left to right on the beach and advancing toward the seaward GCPs. The GCPs on the beach (17–20) are always dry and thus always considered in the alignment, while GCPs 12 and 13 are lying either in a pond or in the deeper section of the channel and are therefore always submerged

<sup>a</sup>For further information on the GCPs' location, see Fig. 2

<sup>b</sup>See Table 1

**Fig. 7 Visual coastline extraction.** An example of aerial images, being used to manually estimate the coastline (yellow lines) in Fig. 3. The images shown here are screenshots from METASHAPE



then subtracted the DEMs of the test flight from the adapted reconstruction of flight 1, yielding a deviation of  $0.4 \pm 0.5$  cm among each other. Both flights were carried out at low-tide. While this test shows that some minor deviations can be expected when reconstructing the same scene with different subsequent flights, we consider these deviations to have no significant influence on our results.

### Dry ground control points

In the manuscript, we consider two survey methods, that have an impact on the alignment procedure in the photogrammetric process. The second approach is done by assuming that only dry areas were accessible and as the water level increases, GCPs becoming wet are neglected in the associated alignment. Table 4 contains all GCPs displayed in Fig. 2 and shows whether they have been dry or submerged in the associated flight set and thus if they have been considered in the alignment procedure.

### Coastline definition

The manuscript contains an areal overview of deviations between the dry and successively submerged reef in Fig. 3.

This figure displays these deviations over the dry reef's orthophoto and—for better orientation—also shows the manually extracted coast- or waterline associated. We defined the waterline by visual observation from the aerial images such as displayed in Fig. 7.

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